# Exercise 16.1

Q.1 Show that the line segment joining the midpoint of opposite sides of a parallelogram divides it into two equal parallelograms.

Given

ABCD is a parallelogram. L is the midpoint of  $\overline{AB}$  and M is the midpoint of  $\overline{DC}$ 

To prove

Area of parallelogram ALMD = area of parallelogram LBCM.



Proof	
Statements	Reasons
AB DC	Opposite sides of parallelogram
	ABCD.
$\overline{AL} \cong \overline{LB} \dots (i)$	L is midpoint of $\overline{AB}$
The parallelograms ALMD and LBCM are on equal	From equation (i)
bases and between the same parallel lines $\overline{AB}$ and	
$\overline{\mathrm{DC}}$	
Hence area of parallelogram ALMD= area of	They have equal areas
parallelogram LBCM.	

Q.2 In a parallelogram ABCD, m $\overline{AB}$  =10cm the altitudes Corresponding to Sides AB and AD are respectively 7cm and 8cm Find  $\overline{AD}$ 

$$\overline{AB} = 10 \text{ cm}$$

$$\overline{DH} = 7$$
cm

$$\overline{MB} = 8$$
cm

$$\overline{AD} = ?$$

Formula

Area of parallelogram = base x altitude

$$\overline{AB} \times \overline{DH} = \overline{AD} \times \overline{IB}$$

$$10 \times 7 = \overline{AD} \times 8$$

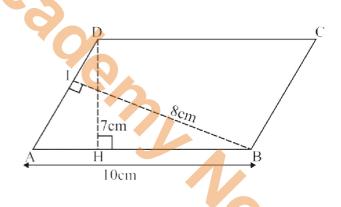
$$\frac{70^{35}}{8^4} = \overline{AD}$$

$$\frac{35}{4} = \overline{AD}$$

$$\overline{AD} = \frac{35}{4}$$

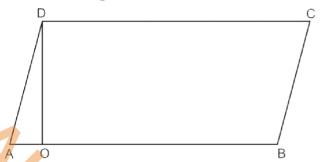
Or

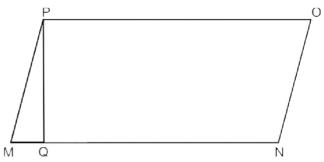
$$\overline{AD} = 8.75$$
cm



В

# Q.3 If two parallelograms of equal areas have the same or equal bases, their altitude are equal





In parallelogram opposite side and opponents angles are Congruent.

# Given

Parallelogram ABCD and parallelogram MNOP

OD is altitude of parallelogram ABCD

PQ is altitude of parallelogram MNOP

Area of ABCD  $\parallel^{gm} \cong Area of MNOP \parallel^{gm}$ 

### To prove

$$\operatorname{m} \overline{OD} \cong \operatorname{m} \overline{PQ}$$

#### Proof

11001	
Statements	Reasons
Area of parallelogram ABCD=	Given
Area of parallelogram MNOP	
Area of parallelogram= base × height	Given
$\overline{AB} \times \overline{OD} = \overline{MN} \times \overline{PQ}$	<b>YO</b> -
We know that	
$\overline{AB} = \overline{MN}$	
So	
$AB \times \overline{OD} = \overline{PO}$	Proved
$\frac{\mathcal{A}\mathcal{B}}{\mathcal{A}\mathcal{B}} \times \overline{\mathrm{OD}} = \overline{\mathrm{PQ}}$	Tioved
$\overline{OD} = \overline{PQ}$	

## **Theorem 16.1.3**

Triangle on the same base and of the same (i.e...equal) altitudes are equal in area

#### Given

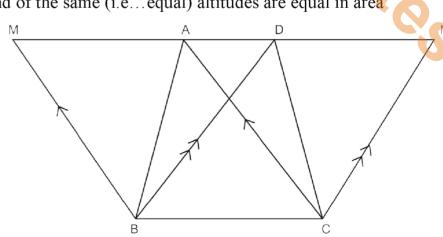
 $\Delta\mbox{'s ABC}$  , DBC on the

Same base  $\overline{BC}$  and

having equal altitudes

#### To prove

Area of  $(\Delta ABC)$  = area of  $(\Delta DBC)$ 



#### **Construction:**

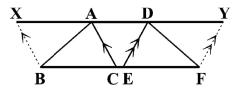
Draw  $\overline{BM} \parallel \text{to} \overline{CA}, \overline{CN} \parallel \text{to} \overline{BD}$  meeting  $\overline{AD}$  produced in M.N.

#### **Proof**

Statements	Reasons
$\Delta ABC$ and $\Delta DBC$ are between the same $\parallel^s$	Their altitudes are equal
Hence MADN is parallel to $\overline{BC}$	
∴ Area    gm (BCAM)= Area    gm (BCND)	These gm are on the same base
But $\triangle ABC = \frac{1}{2} \parallel^{gm} (BCAM)(ii)$	$\overline{BC}$ and between the same $\ ^{s}$
And $\Delta DBC = \frac{1}{2} \parallel^{gm} (BCND)$ (iii)	Each diagonal of a    gm
Hence area ( $\triangle ABC$ ) = Area( $\triangle DBC$ )	Bisects it into two congruent triangles
	From (i) (ii) and (iii)

#### **Theorem 16.1.4**

Triangles on equal bases and of equal altitudes are equal in area.



#### Given

 $\Delta$ s ABC, DEF on equal bases  $\overline{BC}$ ,  $\overline{EF}$  and having altitudes equal

# To prove

Area (
$$\triangle$$
ABC) = Area ( $\triangle$ DEF)

#### **Construction:**

Place the  $\Delta s$  ABC and DEF so that their equal bases  $\overline{BC}$  and  $\overline{EF}$  are in the same straight line BCEF and their vertices on the same side of it .Draw  $\overline{BX}$   $\|\overline{CA}$  and  $\overline{FY}$ 

 $\|\overline{ED}$  meeting  $\overline{AD}$  produced in X, Y respectively

#### **Proof**

Statements	Reasons
$\Delta ABC$ , $\Delta DEF$ are between the same parallels	Their altitudes are equal (given)

∴ XADY is  $\parallel^{gm}$  to BCEF

∴ area  $\|^{gm}$  (BCAX) = A area  $\|^{gm}$  (EFYD)----(i)

These  $\|^{gm}$  are on equal bases and between

the same parallels

Diagonal of a gm bisect it

But  $\triangle ABC = \frac{1}{2} \parallel^{gm} (BCAX) ---- (ii)$ 

And area of  $\Delta DEF = \frac{1}{2}$  area of  $\parallel^{gm}$  (EFYD)\_ (iii)

 $\therefore area (\Delta ABC) = area (\Delta DEF)$ 

From (i),(ii)and(iii) Science academy Notes