

## Exercise 2.1

**Q.1** Identify which of the following are rational and irrational numbers?

- (i)  $\sqrt{3}$  Irrational number
- (ii)  $\frac{1}{6}$  Rational number
- (iii)  $\pi$  Irrational number
- (iv)  $\frac{15}{2}$  Rational number
- (v) 7.25 Rational number
- (vi)  $\sqrt{29}$  Irrational number

**Q.2** Convert the following fractions into decimal fractions.

(i)  $\frac{17}{25}$

**Solution:**  $\frac{17}{25}$

$$\begin{array}{r} 0.68 \\ 25 \overline{) 170} \\ \underline{-150} \\ 200 \\ \underline{-200} \\ 0 \end{array}$$

$\frac{17}{25} = 0.68$  **Ans**

(ii)  $\frac{19}{4}$

**Solution:**  $\frac{19}{4}$

$$\begin{array}{r} 4.75 \\ 4 \overline{) 19.000} \\ \underline{16} \\ 30 \\ \underline{28} \\ 20 \\ \underline{20} \\ 0 \end{array}$$

$= \frac{19}{4}$   
 $= 4.75$  **Ans**

(iii)  $\frac{57}{8}$

**Solution:**  $\frac{57}{8}$

$$\begin{array}{r} 7.125 \\ 8 \overline{) 57} \\ \underline{-56} \\ 10 \\ \underline{8} \\ 20 \\ \underline{-16} \\ 40 \\ \underline{40} \\ 0 \end{array}$$

$= \frac{57}{8}$   
 $= 7.125$  **Ans**

(iv)  $\frac{205}{18}$

**Solution:**  $\frac{205}{18}$

$$\begin{array}{r} 11.388 \\ 18 \overline{) 205.000} \\ \underline{25} \end{array}$$

$$\begin{array}{r} 18 \\ \underline{70} \\ -54 \\ \underline{160} \\ -144 \\ \underline{160} \\ -144 \\ \underline{16} \end{array}$$

$$\begin{array}{r} 208 \\ \underline{18} \\ = 11.3888 \\ = 11.3889 \text{ Ans} \end{array}$$

(v)  $\frac{5}{8}$

Solution:  $\frac{5}{8}$

$$\begin{array}{r} .625 \\ 8 \overline{) 5.000} \\ \underline{48} \\ 20 \\ \underline{-16} \\ 40 \\ \underline{-40} \\ 0 \end{array}$$

$$\begin{array}{r} 5 \\ \underline{8} \\ = 0.625 \text{ Ans} \end{array}$$

(vi)  $\frac{25}{38}$

Solution:  $\frac{25}{38}$

$$\begin{array}{r} 0.65789... \\ 38 \overline{) 250} \\ \underline{-228} \\ 220 \\ \underline{-190} \\ 300 \\ \underline{-266} \\ 340 \\ \underline{-304} \\ 360 \\ \underline{-342} \\ 18 \end{array}$$

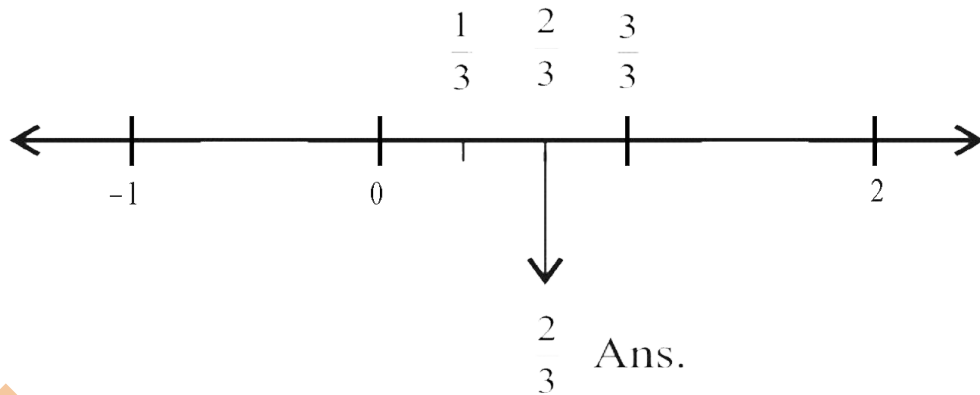
$$\begin{array}{r} 25 \\ \underline{38} \\ = 0.65789 \text{ Ans} \end{array}$$

**Q.3** Which of the following statements are true and which are false?

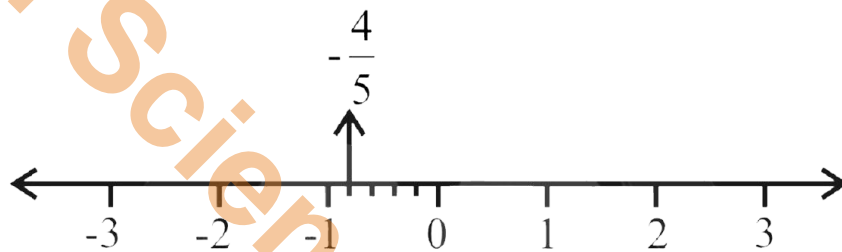
- |       |  |       |
|-------|--|-------|
| (i)   | $\frac{2}{3}$ is an irrational number.   | False |
| (ii)  | $\pi$ is an irrational number.           | True  |
| (iii) | $\frac{1}{9}$ is a terminating fraction. | False |
| (iv)  | $\frac{3}{4}$ is a terminating fraction. | True  |
| (v)   | $\frac{4}{5}$ is a recurring fraction.   | False |

**Q.4** Represent the following numbers on the number line.

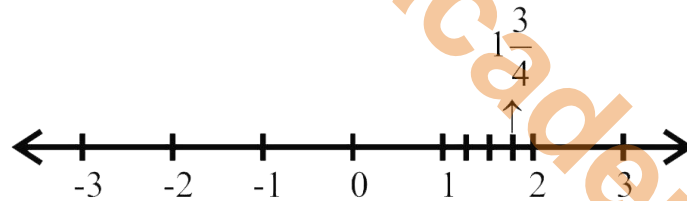
(i)  $\frac{2}{3}$



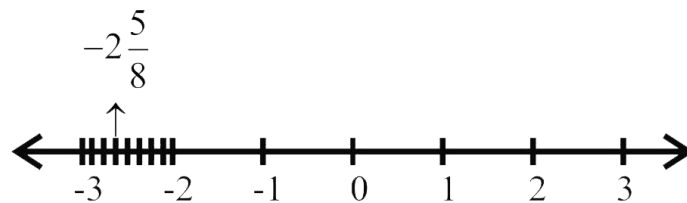
(ii)  $-\frac{4}{5}$



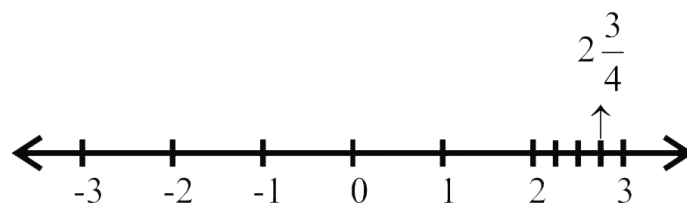
(iii)  $1\frac{3}{4}$



(iv)  $-2\frac{5}{8}$



(v)  $2\frac{3}{4}$



(vi)  $\sqrt{5}$

By Pythagoras theorem

$$(\text{Hypotenus})^2 = (\text{Base})^2 + (\text{Perpendicular})^2$$

$$(\overline{OB})^2 = (2)^2 + (1)^2$$

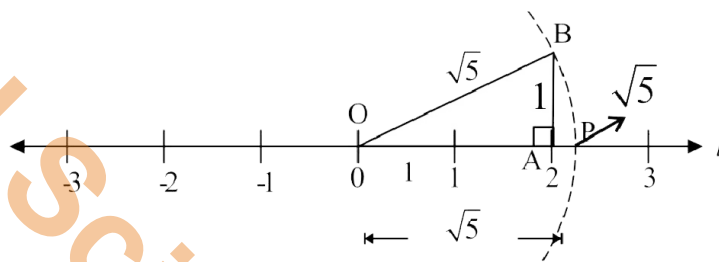
$$(\overline{OB})^2 = 4 + 1$$

$$(\overline{OB})^2 = 5$$

Taking square root on both sides

$$\sqrt{(\overline{OB})^2} = \sqrt{5}$$

$$\overline{OB} = \sqrt{5}$$



**Q.5** Give a rational number between

$$\frac{3}{4} \text{ and } \frac{5}{9}$$

**Solution:**

Required No between

$$\frac{3}{4} \text{ and } \frac{5}{9}$$

$$= \left[ \frac{3}{4} + \frac{5}{9} \right] \div 2$$

$$= \left[ \frac{27 + 20}{36} \right] \div 2$$

$$= \left[ \frac{47}{36} \right] \div 2$$

$$= \frac{47}{36} \times \frac{1}{2}$$

$$= \frac{47}{72} \text{ Ans}$$

**Q.6** Express the following recurring decimals as the rational number

$$\frac{p}{q} \text{ where } p, q \text{ are integer}$$

and  $q \neq 0$ .

(i)  $0.\overline{5}$

**Solution:**

$$x = 0.\overline{5}$$

$$x = 0.555\dots$$

$$10 \times x = 10 \times 0.555\dots$$

$$10x = 5.555\dots$$

$$10x = 5 + 0.555\dots$$

$$10x = 5 + x$$

$$10x - x = 5$$

$$9x = 5$$

$$x = \frac{5}{9}$$

$$\therefore 0.\overline{5} = \frac{5}{9} \text{ Ans}$$

(ii)  $0.\overline{13}$

**Solutions:**

Suppose

$$x = 0.\overline{13}$$

$$x = 0.131313\dots$$

$$100x = 100 \times 0.131313\dots$$

$$100x = 13.1313\dots$$

$$100x = 13 + 0.1313\dots$$

$$100x = 13 + x$$

$$100x - x = 13$$

$$99x = 13$$

$$x = \frac{13}{99}$$

$$\therefore 0.\overline{13} = \frac{13}{99} \text{ Ans}$$

(iii)  $0.\overline{67}$

**Solutions:**

Suppose

$$x = 0.\overline{67}$$

$$x = 0.676767\dots$$

$$100x = 100 \times 0.676767\dots$$

$$100x = 67.6767\dots$$

$$100x = 67 + 0.6767\dots$$

$$100x = 67 + x$$

$$100x - x = 67$$

$$99x = 67$$

$$x = \frac{67}{99}$$

$$\therefore 0.\overline{67} = \frac{67}{99} \text{ Ans}$$